# Protocols for Authenticated Oblivious Transfer

Mehrad Jaberi and Hamid Mala

Abstract— Oblivious transfer (OT) is a basic building block in many cryptographic protocols. A common approach in designing secure multiparty computation protocols is to assume that messages of the protocol are being transmitted over an authenticated channel, where entities have been authenticated to each other before the actual flows of the protocol. However, the mentioned aspect leads to some restrictions in design and development of secure multiparty computations. In this paper, we exploit some well-known authenticated Diffie-Hellman-based key exchange protocols to build three authenticated 1-out-of-2 oblivious transfer protocols. As a result, our schemes incorporate the authentication within the oblivious transfer protocol itself, instead of performing authentication via a separate sub-protocol. We show that the proposed protocols are secure in the semihonest model. We also compare our new schemes with the previous methods (performing authentication via a separate subprotocol) which illustrates that our schemes decrease computational and communication complexity for both sender and receiver.

Index Terms— oblivious transfer, OT, secure computation, authentication, key exchange

## I. INTRODUCTION

OBlivious transfer (OT) is a basic cryptographic protocol and it is used as a core building block in secure multiparty computations (MPC). The simplest form of OT, which is called 1-out-of-2 OT, is a protocol in which the sender has two secrets  $m_0$ ,  $m_1$  and the receiver has a select bit sb. The sender has no output at the end of the protocol, while the receiver learns  $m_{sb}$ . Our proposed schemes are 1-out-of-2 OT protocols.

Considering the importance of OT and its key role in cryptographic applications, it is vital to introduce secure and efficient OT protocols. On the other hand, since OT is being used usually as a black-box, it is essential for the involved parties to be authenticated. A common approach in designing MPC protocols including OT, is to impose the authentication to a separate protocol and assume that the actual MPC protocol is being proceed in an ideal authenticated channel. This means that the authentication must be guaranteed by some external mechanism. As a matter of fact, the mentioned approach leads to create some limitations in design and

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analysis of MPC protocols, since it treats authentication as a pre-requisite module for any rational solution to MPC protocols. Hence, in [1] a methodology have been provided based on incorporating the authentication within the protocol itself, rather than imposing authentication to a separate prerequisite phase. In this paper, we introduce three simple, secure and time efficient OT protocols. Despite previous key exchange based schemes, our OT protocols are authenticated as well. In fact, in our schemes, we did not impose authentication to an external mechanism. We exploit the most Diffie-Hellman based authenticated agreement schemes (KAS) including STS [2], MTI [3] and Girault KAS [4] to construct new authenticated OTs. Our schemes are more efficient in terms of computational and communication complexity.

Related work. Since 1981[5], where Rabin introduced the notion of OT (another similar concept had been proposed in 1970 under the name of "conjugate coding" [6]), there have been many papers proposing new OT protocols or trying to optimize earlier ones [7,8,9,10]. The two notable protocols that are similar to ours, are [11] and [10], which are not as efficient as our schemes. Like our proposed protocols, [11] and [10] have been also constructed by exploiting Diffie-Hellman KAS. On the other hand, [12,13,14] tried to construct OT protocols as secure as possible. The recent effort has been made in [7] where Diffie-Hellman KAS [15] was used to construct an efficient OT. Note that the OT proposed in [7] is not authenticated, while our proposed protocols are authenticated using certifications signed by a trusted authority.

**OT extension.** Analogous to hybrid encryption systems, where two entities use public-key cryptography to share a symmetric-key and then use a symmetric encryption (e.g. AES) for further data communication, OT protocols can also be extended. In OT extension, entities generate few "seed" OTs based on public-key schemes, and then extend these base OTs to any number of OTs required, using symmetric-key schemes. [8], [9] are two efficient examples for OT extension. Based on [7], we believe that our schemes can be very useful, efficient and simple OTs for being employed as seed OTs in OT extension.

**Paper organization.** The rest of this paper is organized as follows. In Section II, we propose our three authenticated OT schemes. In Section III, we discuss about the security of our proposed schemes. In Section IV, a comparison between our schemes and previous methods is presented. Finally, we conclude the paper in Section V.

#### II. THE PROPOSED PROTOCOLS

In this section, we propose three authenticated OT protocols. These protocols are based on three authenticated KAS. In fact, we exploit Station-to-Station (STS) KAS [2], MTI KAS [3] and Girault KAS [4]. In our protocols, U and V are sender and receiver, respectively, where U owns two secrets  $m_0$  and  $m_1$ . At the end of the protocol, V obtains either  $m_0$  or  $m_1$  while U learns nothing. U and V agree on  $H(\cdot)$ , a secure hash function, and a symmetric-key encryption algorithm such as AES-128.

In STS-based OT and MTI-based OT, suppose that p is a large prime number and all the operations are in  $\mathbb{Z}_p$  and g is a generator of the multiplicative group  $\mathbb{Z}_p^*$ .

## A. STS-based OT

Fig. 1, shows our STS-based oblivious transfer scheme. U chooses  $a_U$ , a random element of  $\mathbb{Z}_p^*$  and sends  $b_U = g^{a_U}$  along with her certificate Cert(U) to V, where

$$Cert(U) = (ID(U), ver_U, Sig_{TA}(ID(U), ver_U))$$

 $ver_U$  is a verification algorithm for the signature scheme of Uand  $Sig_{TA}$  is the signature of the TA which is verifiable for everyone. V chooses  $a_V$  at random from  $\mathbb{Z}_p^*$ . If his select bit sb = 0, then he computes  $b_V = g^{a_V}$ , otherwise he computes  $b_V = b_U g^{a_V}$ . Then he computes  $K_V = H(b_U^{a_V}) = H(g^{a_U a_V})$ and  $y_V = Sig_V(ID(U) \parallel b_V \parallel b_U)$ . He sends  $b_V$  and  $y_V$  along with his certificate Cert(V) to U. Then U verifies  $y_V$  using  $ver_V$ . If the signature  $y_V$  is not valid, she rejects. Otherwise she computes  $k_0 = H(b_V^{a_U})$ ,  $k_1 = H(\left(\frac{b_V}{b_U}\right)^{a_U})$  and  $y_U =$  $Sig_U(ID(V) \parallel b_U \parallel b_V)$ . Then she encrypts  $m_0$  and  $m_1$  with  $k_0$  and  $k_1$ , respectively and forms  $e_0 = E_{k_0}(m_0)$  and  $e_1 =$  $E_{k_1}(m_1)$  where  $E_{\lambda}(\rho)$  is the symmetric encryption of massage  $\rho$  with key  $\lambda$ . Now, U sends  $e_0$  and  $e_1$  along with  $y_U$  to V. Vverifies  $y_U$  using  $ver_V$ . If the signature  $y_U$  is not valid he rejects; otherwise he decrypts  $e_{sb}$  with his key  $K_V$ . Note that he can decrypt both  $e_0$  and  $e_1$  but only one of them is meaningful. As it will be discussed in Section III, the security of the scheme is based on intractability of the CDH problem.

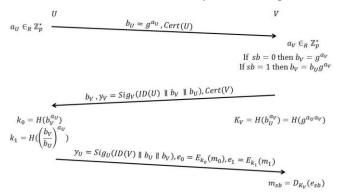


Fig. 1. The proposed STS-based OT

## B. MTI-based OT

The proposed MTI-based OT is shown in Fig. 2 and Fig. 3. Although MTI is a set of several key agreement schemes, we chose MTI/A0 which we believe is the most well-known one.

Other MTI schemes will be exploitable to construct OT protocols using the same approach.

**Public-key generation.** First, each user T chooses a random element  $a_T$  from  $\mathbb{Z}_p^*$  and computes  $b_T = g^{a_T}$ . Then T sends g and  $b_T$  to the TA. TA computes the user's certificate Cert(T) from which  $b_T$  can be obtained and sends Cert(T) to T. This phase can be operated offline.

$$a_T \in_R \mathbb{Z}_p^* \xrightarrow{T} b_T = g^{a_T}, g$$

$$Cert(T) = (ID(T), b_T, g, Sig_{TA}(ID(T), b_T, g))$$

Fig. 2. The proposed MTI-based OT, public key generation phase

The main MTI-based OT protocol. Since the MTI-based OT is very similar to the proposed STS-based OT, we abridge the explanation. Note that in the original MTI KAS, the mutual key of users U and V is computed as  $K = g^{r_U a_V + r_V a_U}$ , where  $r_T$  is a random element of  $\mathbb{Z}_p^*$  chosen by user T in the beginning of the protocol. Hence in our MTI-based OT protocol  $K_V = H(s_U^{a_V} b_U^{r_V}) = H(g^{r_U a_V + r_V a_U})$  and the keys generated by the sender are  $k_0 = H(s_V^{a_U} b_V^{r_U})$  and  $k_1 = H(\frac{s_V^{a_U} b_V^{r_U}}{s_U^{a_U}})$  where  $s_T = g^{r_T}$ . This protocol has been shown in Fig. 3.

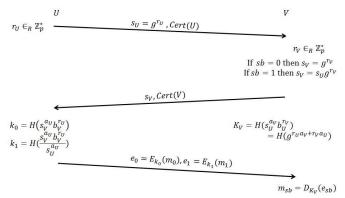


Fig. 3. The proposed MTI-based OT

## C. Girault-based OT

Girault is a self-certifying KAS. We introduce our Girault-based OT protocol in two phases: "the public key generation" and "the main protocol". Girault combines features of both RSA and discrete logarithm problem. Suppose n = pq, where p and q are two large primes and g is a generator of the multiplicative group  $\mathbb{Z}_n^*$ . n and g are public but p and q are secret to the TA. On the other hand, TA chooses a public RSA exponent e and the corresponding secret exponent d where  $d = e^{-1} \mod \varphi(n)$ .

**Public key generation.** Each user T chooses a random number  $a_T \in \mathbb{Z}_n^*$  and computes  $b_T = g^{a_T} \bmod n$ . Then T sends  $a_T$  and  $b_T$  to the TA through a secure channel. TA checks whether  $b_T$  is equal to  $g^{a_T} \bmod n$  or not. If not, TA rejects;

otherwise it computes  $p_T = (b_T - ID(T))^d \mod n$  and sends  $p_T$  to T. This protocol has been shown in Fig. 4.

$$a_T \in_{\mathbb{R}} \mathbb{Z}_n^* \xrightarrow{T} b_T = g^{a_T} \bmod n, a_T$$
 Checks whether  $b_T = g^{a_T} \bmod n$  
$$p_T = (b_T - ID(T))^d \bmod n$$

Fig. 4. The Girault-based OT, public key generation phase

The main Girault-based OT protocol. U chooses  $r_U$  at random from  $\mathbb{Z}_n^*$  and computes  $s_U = g^{r_U} \mod n$  and sends  $s_U$  along with the ID(U) and  $p_U$  to V. Then, V, the receiver, chooses  $r_V$  at random from  $\mathbb{Z}_n^*$ . If his select bit sb is 0, then he computes  $s_V = g^{r_V} \mod n$ . Otherwise he computes  $s_V = s_U g^{r_V} \mod n$  and  $K_V = H(s_U^{a_V}(p_U^e + ID(U))^{r_V} \mod n)$ . Then V sends  $s_V$  and ID(V) and  $p_V$  to U. The sender U computes  $k_0 = H(s_V^{a_U}(p_V^e + ID(V))^{r_U} \mod n)$  and  $k_1 = H(s_V^{a_U}(p_V^e + ID(V))^{r_U} \mod n)$  and encrypts  $m_0$  and  $m_1$  by the keys  $k_0$  and  $k_1$ , respectively. U sends  $e_0 = E_{k_0}(m_0)$  and  $e_1 = E_{k_1}(m_1)$  to V. Finally, V decrypts  $e_{sb}$  and obtains  $m_{sb}$ . Our proposed Girault-based OT has been shown in Fig. 5.

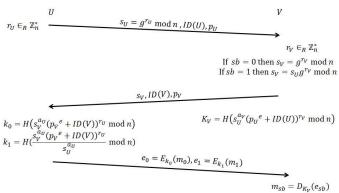


Fig. 5. The proposed Girault-based OT

#### III. SECURITY OF OUR PROPOSED SCHEMES

In this section, we discuss the security of our OT schemes in the semi-honest model. Hence, we explain that in our schemes, the sender U cannot guess the select bit of the receiver V with the probability more than 1/2 and V can just decrypt one of the ciphertexts. In the following discussion, by  $CDH(g^a, g^b, g)$  we denote the computational Diffie-Hellman problem. This problem states that "given g, the generator of a multiplicative group G,  $g^a$  and  $g^b$ , compute  $g^{ab}$ ."

**Security of the STS-based OT.** In the STS-based OT, since  $a_V$  is secret, U cannot distinguish between  $g^{a_V}$  and  $b_U g^{a_V}$ . In other words, when  $a_V$  is chosen uniformly at random from  $\mathbb{Z}_p^*$ , for any  $b_U$  in G the distribution of  $g^{a_V}$  and  $b_U g^{a_V}$  are the same.

On the other hand, to learn both  $m_0$  and  $m_1$ , V has to compute  $b_U^{a_U}$ . Thus, he needs to know  $a_U$ . Hence, V needs to solve the CDH problem  $CDH(b_U, b_U, g)$ .

**Security of the MTI-based OT.** In the MTI-based OT, each user T has two random elements  $a_T$  and  $r_T$  which are secret. Similar to the STS-based OT, since  $r_V$  is secret,  $g^{r_V}$  and  $s_U g^{r_V}$  are indistinguishable for U.

Likewise, to decrypt both of  $e_0$  and  $e_1$ , V has to compute  $s_U^{a_U}$  (or  $b_U^{r_U}$ ) where he needs either  $a_U$  or  $r_U$ . Thus, V should solve  $CDH(s_U, b_U, g)$ .

**Security of the Girault-based OT.** Same as the MTI-based OT,  $g^{r_V}$  and  $s_U g^{r_V}$  are indistinguishable for U, since  $r_V$  is a random secret.

On the other hand, to learn both secrets  $m_0$  and  $m_1$ , V should learn either  $a_U$  or  $r_U$ . Thus, V should solve the CDH problem  $CDH(s_U, b_U, g)$ . Note that  $b_U = p_U^e + ID(U) \mod n$ .

#### IV. COMPARISON RESULTS

In this section, we compare our three proposed protocols with previous schemes where authentication is being imposed to a separate module, in terms of computational and communication complexity. Building an authenticated channel before the actual flows of the protocol means running an authenticated key agreement scheme e.g. STS, and then using the resulted STS key to encrypt the OT messages. We suppose that the OT protocol is the protocol proposed in [7], since it is the most efficient OT protocol up until now in terms of computational and communication complexity. We also suppose that the authentication channel is being built by STS-KAS[2], MTI-KAS[3] and Girault-KAS[4], since the mentioned schemes guaranty the authentication just with either one more message signing or two more exponentiations, compared to the basic Diffie-Hellman KAS. As it is shown in TABLE 1, using our schemes is more efficient in terms of computational and communication complexity for both sender and receiver. Since, incorporation authentication and OT makes the overall scheme more efficient.

TABLE I
Comparison between the proposed OT schemes and previous methods

Protocol	Computational Complexity of Sender				Computational Complexity of Receiver				Number of
	Exp.	Hash	Enc	Sig	Exp.	Hash	Enc	Sig	messages
first STS, then OT	5	3	5	2	4	2	4	2	6
STS-based OT	3	2	2	2	2	1	1	2	3
first MTI, then OT	6	3	5	0	5	2	4	0	5
MTI-based OT	4	2	2	0	3	1	1	0	3
first Girault, then OT	7	3	5	0	6	2	4	0	5
Girault-based OT	5	2	2	0	4	1	1	0	3

### V. CONCLUSION

In this paper, we introduced three authenticated oblivious transfer schemes by exploiting the most well-known Diffie-Hellman-based key exchange schemes namely, STS, MTI and Girault. Comparison among our proposed protocols and previous schemes shows that incorporating authentication with oblivious transfer makes the protocol more efficient for both sender and receiver. Note that for performance optimization, instead of intensive exponential operations, we can use elliptic curve computations. Our future work would be manipulating other key exchange schemes to gain more efficient OT protocols.

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